

Math 1392 - Trigonometry

Fall 2015

Practice Test 1 on Chapters 1 and 2

Instructions: Calculators are allowed on this test. Each problem is worth 7 points.

1. Find smallest positive angle that is coterminal with each of the following angles:

a) -140° c) $5\pi/4$

b) 610° d) $-5\pi/3$

2. Convert the following radian measures to degrees:

a) $\frac{7\pi}{6}$ b) $\frac{9\pi}{20}$

3. Convert the following degrees to radian measures:

a) 280° b) -150°

4. Perform the following conversions:

a) Convert 40 rev/min to radians/sec

b) Convert $90^\circ/\text{min}$ to radians/hr

c) Convert 6π radians/hr to $^\circ/\text{min}$

5. A bicycle tire rotates at a rate of 3 revolution per second. What is its angular velocity in radians/minute? If the tire has a diameter of 20 inches, what is the linear velocity of the bicycle in feet/minute? (Recall: $v = \omega r$.)

6. Evaluate the following trigonometric functions using a circle chart

a) $\sin(-\pi/3)$ d) $\sin(225^\circ)$

b) $\cos(\pi/4)$ e) $\tan(-240^\circ)$

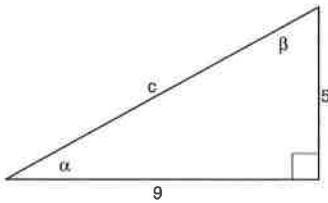
c) $\tan(5\pi/6)$ f) $\cos(120^\circ)$

7. Evaluate the following values by determining the value of the trigonometric functions and simplifying the result:

a) $\sin(\pi/6) * \sin(\pi/4) - \cos(\pi/6) \cos(\pi/4)$

b) $\sin(3\pi/4) * \tan(3\pi/4) + \cos(3\pi/4)$

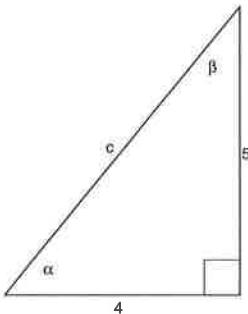
8. Determine the six trigonometric functions given the sides in the following triangles:



a)

$$\cos(\alpha) = \text{_____} \quad \sin(\alpha) = \text{_____} \quad \tan(\alpha) = \text{_____}$$

$$\sec(\alpha) = \text{_____} \quad \csc(\alpha) = \text{_____} \quad \cot(\alpha) = \text{_____}$$



b)

$$\cos(\alpha) = \text{_____} \quad \sin(\alpha) = \text{_____} \quad \tan(\alpha) = \text{_____}$$

$$\sec(\alpha) = \text{_____} \quad \csc(\alpha) = \text{_____} \quad \cot(\alpha) = \text{_____}$$

9. A person measures the angle of elevation of a tall building at 63° while standing 280 feet from the base of the building. How tall is the building?

10. You and a friend are on opposite sides of the Arkansas river, directly opposite each other. Your friend walks 50 feet in a direction parallel to the river. If you measure an angle of 18° between your friend's original position and your friend's new position, how wide is the Arkansas river?

11. Simplify the following expressions completely:

a) $\tan(x) - \sin(x) \sec(x)$

b) $\cos(x) \sin(x) \tan(x) + \sin(x) \cos(x) \cot(x)$

c) $\frac{\cos^2(x)}{1 - \sin(x)}$

12. Given that $\cos(\alpha) = 2/5$ and α is in Quadrant IV, determine the value of $\sin(\alpha)$ and $\tan(\alpha)$.

13. Simplify the following expression completely (The answer is one of the six trigonometric functions (i.e., $\sin(x)$, $\cos(x)$, $\tan(x)$, $\csc(x)$, $\sec(x)$ or $\cot(x)$).

$$\frac{\cot(x)}{\csc(x) - \sin(x)}$$

14. Simplify the following expression completely (The answer is one of the six trigonometric functions (i.e., $\sin(x)$, $\cos(x)$, $\tan(x)$, $\csc(x)$, $\sec(x)$ or $\cot(x)$).

$$\frac{\sin^2(x) \sec(x)}{\csc(x)} + \tan(x) \cos^2(x)$$

$$1.a \quad \begin{array}{r} -140^\circ \\ + 360^\circ \\ \hline 220^\circ \end{array}$$

$$b. \quad \begin{array}{r} 610^\circ \\ - 360^\circ \\ \hline 250^\circ \end{array}$$

$$c. \quad \frac{5\pi}{4} \cancel{- \frac{8\pi}{4}}$$

This is
Smallest positive
angle

$$d. \quad -\frac{5\pi}{3} + 2\pi$$

$$-\frac{5\pi}{3} + \frac{6\pi}{3} = \frac{\pi}{3}$$

$$2a. \quad \begin{array}{r} 300^\circ \\ 60^\circ \\ \hline 360^\circ \\ \cancel{2\pi} \end{array} = 210^\circ$$

$$b. \quad \begin{array}{r} 9\pi \\ \hline 20 \\ \cancel{2\pi} \end{array} \frac{360^\circ}{18} = 81^\circ$$

$$3a. \quad \begin{array}{r} 14 \\ 280^\circ \\ \hline 360^\circ \\ \cancel{4} \end{array} \cdot \frac{2\pi}{\cancel{360^\circ}} = \frac{14\pi}{9}$$

$$b. \quad -180^\circ \cdot \frac{2\pi}{\cancel{360^\circ}} = -\frac{5\pi}{6}$$

$$4a. \quad \begin{array}{r} 40 \frac{\text{rev}}{\text{min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} \cdot \frac{2\pi \text{ rad}}{1 \text{ rev}} \\ \hline 3 \end{array} = \frac{4\pi}{3} \frac{\text{rad}}{\text{sec}}$$

$$b. \quad \begin{array}{r} 30 \\ \frac{90^\circ}{\text{min}} \cdot \frac{60 \text{ min}}{1 \text{ hr}} \cdot \frac{2\pi \text{ rad}}{360^\circ} \\ \hline 6 \end{array} = 30\pi \frac{\text{rad}}{\text{hr}}$$

$$c. \quad \begin{array}{r} 6\pi \frac{\text{rad}}{\text{hr}} \cdot \frac{1 \text{ hr}}{60 \text{ min}} \cdot \frac{60^\circ}{2\pi \text{ rad}} \\ \hline 30 \end{array} = 180^\circ/\text{min}$$

$$5. \quad \omega = \frac{3 \frac{\text{rev}}{\text{sec}}}{\cancel{sec}} \cdot \frac{2\pi \text{ rad}}{1 \text{ rev}} \cdot \frac{60 \text{ sec}}{1 \text{ min}} = 360\pi \frac{\text{rad}}{\text{min}} \quad r = 10 \text{ in}$$

$$v = \omega \cdot r = \frac{360\pi}{\text{min}} \frac{\text{rad}}{\cancel{min}} \cdot \frac{10 \text{ in}}{1} \cdot \frac{1 \text{ ft}}{12 \text{ in}} = 300\pi \frac{\text{ft}}{\text{min}}$$

$$6a. \quad -\frac{\sqrt{3}}{2} \quad d. \quad -\frac{\sqrt{2}}{2}$$

$$b. \quad \frac{\sqrt{2}}{2} \quad e. \quad -\sqrt{3}$$

$$c. \quad -\frac{1}{\sqrt{3}} = -\frac{\sqrt{3}}{3} \quad f. \quad -\frac{1}{\sqrt{2}} = -\frac{\sqrt{2}}{2}$$

$$7a. \frac{1}{2} \cdot \frac{\sqrt{2}}{2} - \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{2}}{2} = \frac{\sqrt{2} - \sqrt{6}}{4}$$

$$b. \frac{\sqrt{2}}{2} \cdot (-1) - \frac{\sqrt{2}}{2} = -\sqrt{2}$$

$$8a. C^2 = 5^2 + 9^2 = 25 + 81 = 106$$

$$C = \sqrt{106}$$

$$\cos \alpha = \frac{9}{\sqrt{106}}$$

$$\sin \alpha = \frac{5}{\sqrt{106}}$$

$$\tan \alpha = \frac{5}{9}$$

$$\sec \alpha = \frac{\sqrt{106}}{9}$$

$$\csc \alpha = \frac{\sqrt{106}}{5}$$

$$\cot \alpha = \frac{9}{5}$$

$$b. C^2 = 4^2 + 5^2 = 41$$

$$C = \sqrt{41}$$

$$\cos \alpha = \frac{4}{\sqrt{41}}$$

$$\sin \alpha = \frac{5}{\sqrt{41}}$$

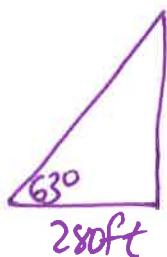
$$\tan \alpha = \frac{5}{4}$$

$$\sec \alpha = \frac{\sqrt{41}}{4}$$

$$\csc \alpha = \frac{\sqrt{41}}{5}$$

$$\cot \alpha = \frac{4}{5}$$

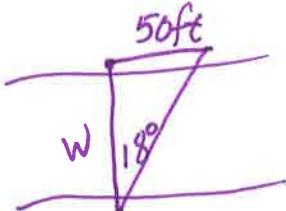
9.



$$\tan 63^\circ = \frac{H}{280 \text{ ft}}$$

$$H = 280 \text{ ft} \cdot \tan 63^\circ \approx 550 \text{ ft}$$

10.



$$\tan 18^\circ = \frac{50}{W}$$

$$W = \frac{50 \text{ ft}}{\tan 18^\circ} \approx 154 \text{ ft}$$

$$11. a \quad \tan x = \frac{\sin x}{\cos x}$$

$$\frac{\sin x}{\cos x} - \frac{\sin x}{1} \cdot \frac{1}{\cos x} = \frac{\sin x}{\cos x} - \frac{\sin x}{\cos x} = 0$$

$$b. \quad \cos x \cdot \sin x \cdot \frac{\sin x}{\cos x} + \sin x \cdot \cos x \cdot \frac{\cos x}{\sin x} = \sin^2 x + \cos^2 x = 1$$

$$c. \quad \frac{\cos^2 x}{1 - \sin x} = \frac{1 - \sin^2 x}{1 - \sin x} = \frac{(1 - \sin x)(1 + \sin x)}{1 - \sin x} = 1 + \sin x$$

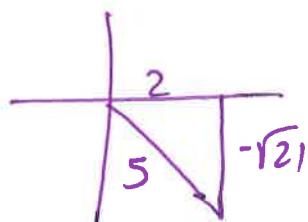
$$12. \quad \cos \alpha = \frac{2}{5}$$

$$2^2 + b^2 = 5^2$$

$$\sin \alpha = -\frac{\sqrt{21}}{5}$$

$$b^2 = 21$$

$$\tan \alpha = -\frac{\sqrt{21}}{2}$$



$$13. \quad \frac{\cot x}{\csc x - \sin x} = \frac{\frac{\cos x}{\sin x}}{\frac{1}{\sin x} - \frac{\sin x}{1} \cdot \frac{\sin x}{\sin x}} = \frac{\frac{\cos x}{\sin x}}{\frac{1 - \sin^2 x}{\sin x}} = \frac{\frac{\cos x}{\sin x}}{\frac{\cos^2 x}{\sin x}} = \frac{\cos x}{\cos^2 x} = \frac{1}{\cos x} = \sec x$$

$$14. \quad \frac{\sin^2 x \sec x}{\csc x} + \tan x \cos^2 x = \frac{\sin^2 x \cdot \frac{1}{\cos x}}{\frac{1}{\sin x}} + \frac{\sin x}{\cos x} \cdot \frac{\cos^2 x}{1}$$

$$\frac{\sin^2 x}{\cos x} \cdot \frac{\sin x}{1} + \frac{\sin x}{\cos x} \cdot \frac{\cos^2 x}{1} = \frac{\sin^3 x + \sin x \cos^2 x}{\cos x} = \frac{\sin x (1 + \sin^2 x)}{\cos x} = \frac{\sin x}{\cos x} = \tan x$$