

Solutions of Self-test 1 of Chapter 3

1. **Chapter 4 Review Exercises 4.** $\int \frac{4}{x^2} dx = 4 \int x^{-2} = -4x^{-1} + c.$
2. **Chapter 4 Review Exercises 8.** $\int 3\sqrt{x} dx = 3 \int x^{1/2} = 2x^{3/2} + c.$
3. **Chapter 4 Review Exercises 10.** $u = x^2 + 4, du = 2x dx, x dx = \frac{1}{2} du. \int \frac{x}{x^2 + 4} dx = \frac{1}{2} \int \frac{1}{u} du = \frac{1}{2} \ln |u| + c = \frac{1}{2} \ln |x^2 + 4| + c.$
4. **Chapter 4 Review Exercises 15.** $u = x^3, du = 3x^2 dx, x^2 dx = \frac{1}{3} du. \int 6x^2 \cos x^3 dx = 3 \int \cos u du = 3 \sin u + c = 3 \sin x^3 + c.$
5. **Chapter 4 Review Exercises 18.** $u = \ln x, du = \frac{1}{x} dx. \int \frac{\ln x}{x} dx = \int u du = \frac{1}{2} u^2 + c = \frac{1}{2} (\ln x)^2 + c.$
6. **Chapter 4 Review Exercises 19.** $u = \cos x, du = -\sin x dx. \int \tan x dx = -\int \frac{1}{u} du = -\ln |u| + c = -\ln |\cos x| + c.$
7. **Chapter 4 Review Exercises 41.** The intersection points with x axis are 0 and 3 which are obtained by setting $3x - x^2 = 0$. So $A = \int_0^3 (3x - x^2) dx = \left(\frac{3}{2}x^2 - \frac{1}{3}x^3\right)_0^3 = \frac{3}{2}3^2 - \frac{1}{3}3^3 = \frac{9}{2}.$
8. **Chapter 4 Review Exercises 48.** $\int_{-1}^1 (x^3 - 2x) dx = \left(\frac{1}{4}x^4 - x^3\right)_{-1}^1 = \left(\frac{1}{4}1^4 - 1^3\right) - \left(\frac{1}{4}(-1)^4 - (-1)^3\right) = -2.$
9. **Chapter 4 Review Exercises 52.** $u = -t^2, du = -2t dt, u(0) = 0, u(1) = -1. \int_0^1 t e^{-t^2} dt = -\frac{1}{2} \int_0^{-1} e^u du = \frac{1}{2} \int_{-1}^0 e^u du = e^u \Big|_{-1}^0 = 1 - e^{-1}.$
10. **Chapter 4 Review Exercises 58.** $u = x/2, du = dx/2, u(-\pi) = -\pi/2, u(\pi) = \pi/2. \int_{-\pi}^{\pi} \cos(x/2) dx = 2 \int_{-\pi/2}^{\pi/2} \cos u du = \sin u \Big|_{-\pi/2}^{\pi/2} = \sin(\pi/2) - \sin(-\pi/2) = 2.$
11. **Chapter 4 Review Exercises 60.** $f'(x) = \sqrt{x^4 + 12x} = 2x\sqrt{x^4 + 1}.$