$\qquad$ Solutions $\qquad$ Trigonometry, Test 1

Calculator Portion: You may use a calculator on this page.

1) Solve the following triangle. (10 points)

$\tan \left(65^{\circ}\right)=\frac{x}{4} \Rightarrow x=8.57$
$4^{2}+8.57^{2}=x^{2} \Rightarrow x=9.45$

Note that there are roughly 12 ways to solve this problem.

2) A 100-ft guy wire is attached to the top of an $88-\mathrm{ft}$ antenna. What angle does the wire make with the ground? (Picture/diagram: 4 points. Answer: 3 points. Supporting work: 3 points)
$\sin ^{-1}\left(\frac{88}{100}\right)=61.6^{\circ}$



Non-Calculator Portion: You may not use a calculator on the rest of the test.
3) In the figure to the right, draw the standard angle and reference triangle. ( $2+3$ points)

4) Find each of the following. Use the axis below to illustrate your supporting work.
(15 points total: 1 point per answer, 4 points per work)
$\sin \left(30^{\circ}\right)=\frac{1}{2}$
$\cos \left(135^{\circ}\right)=-\frac{1}{\sqrt{2}}$
$\tan \left(240^{\circ}\right)=\frac{-\sqrt{3}}{-1}=\sqrt{3}$

5) A wagon wheel has a 8 spokes. The arc length of the wheel between spokes is 12 inches. Draw a diagram and find the radius of the wheel. ( 5 points for the diagram, 5 points for the radius)
$l=\theta r$
$12=\frac{\pi}{4} \cdot r$
$48=\pi r$
$\frac{48}{\pi}=r$


6) On the axis below, graph the function $y=\cos \left(x-\frac{\pi}{2}\right)$. (10 points)

7) It is known that $\sin (\theta)=\frac{1}{2}$. Find $\cos (\theta)$. Show your work. ( $4+6$ points)
$\cos (\theta)=\frac{\sqrt{3}}{2}$ if $\theta$ comes from the triangle on the right. $\cos (\theta)=-\frac{\sqrt{3}}{2}$ if $\theta$ comes from the triangle on the left.

Or another way to solve this would be to usethe fundamental identity:
$\left(\frac{1}{2}\right)^{2}+\cos ^{2}(\theta)=1$
$\cos ^{2}(\theta)=1-\frac{1}{4}=\frac{3}{4}$
$\cos (\theta)= \pm \frac{\sqrt{3}}{2}$

8) On the axis below, sketch the function $y=2 \sin (4(x+2 \pi))+1$. (10 points)

9) Assume $\sin \left(53^{\circ}\right)=\frac{4}{5}$. Find $\sin \left(127^{\circ}\right)$. Show your work. ( $3+7$ pфints)

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\sin \left(127^{\circ}\right)=\frac{4}{5}
$$



10) Assume $\sin \left(53^{\circ}\right)=\frac{4}{5}$. Find $\sin \left(143^{\circ}\right)$. Show your work. ( $3+7$ points) $\sin \left(143^{\circ}\right)=\frac{3}{5}$


