Name $\qquad$ Solutions $\qquad$ Quiz 4, Calculus 1

1) Given the graph of $y=f(x)$ below, sketch the graph of $f^{\prime}(x)$ on the same axis.

2) The distance travelled by of a bicyclist traveling down a hill is given by $f(x)=3 x^{2}$ feet at time $x$, where $s$ is measured in seconds. Velocity is the rate of change of distance. Use the appropriate ideas we've learned in class thus far to find the velocity function of the bicyclist.

$$
\begin{aligned}
& f^{\prime}(x)=\lim _{h \rightarrow 0} \frac{3(x+h)^{2}-3 x^{2}}{h}=\lim _{h \rightarrow 0} \frac{3\left(x^{2}+2 x h+h^{2}\right)-3 x^{2}}{h}=\lim _{h \rightarrow 0} \frac{3 x^{2}+6 x h+3 h^{2}-3 x^{2}}{h} \\
& =\lim _{h \rightarrow 0} \frac{6 x h+3 h^{2}}{h}=\lim _{h \rightarrow 0} 6 x+3 h=6 x
\end{aligned}
$$

$$
f^{\prime}(x)=6 x \text { feet per second }
$$

