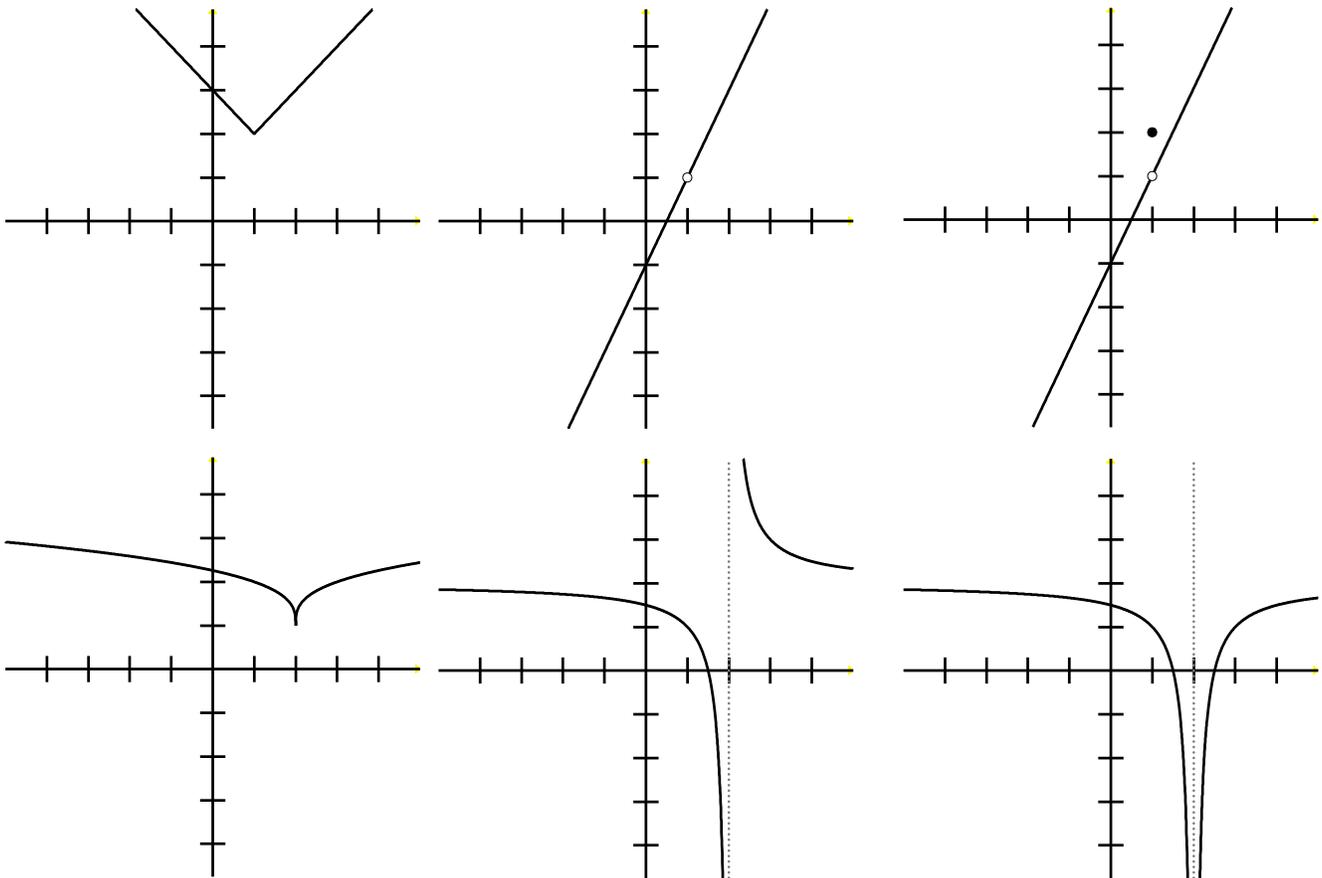


Please show all your work and circle your answer when appropriate. You do not need to simplify answers unless the problem specifies to do so.

1) Find $\frac{1}{\sqrt{x}} \cdot \frac{d}{dx} \left(\frac{1}{\sqrt{x}} \right)$. (6 points)

2) Below are graphs of 6 functions. Some of them are continuous functions on the real line. Some of them are not. Circle those that are continuous. For those that are not continuous, draw a single arrow pointing to a feature of the graph that makes you think it's not continuous. (4 points)



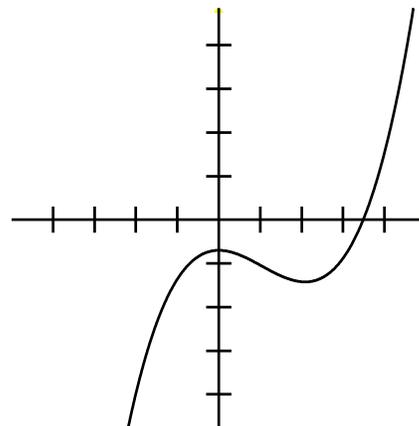
3) Calculate $\lim_{x \rightarrow 1} \frac{5x^2 + 6x + 1}{8x - 4}$ (4 points)

4) Calculate $\lim_{x \rightarrow 1^+} \frac{x - 2}{(x - 1)^3}$ (4 points)

5) Calculate $\lim_{x \rightarrow -2^-} \frac{x^3 - 5x^2 + 6x}{x^4 - 4x^2}$ (4 points)

6) Calculate $\lim_{x \rightarrow -b} \frac{(x+b)^7 + (x+b)^{10}}{4(x+b)}$ (4 points)

7) Given the graph to the right, estimate the average rate of change between the points given by $x = 1$ and $x = 4$. (2 points)



8) Given the graph to the right, estimate the instantaneous rate of change at point given by $x = 1$. (2 points)

9) Find $\lim_{x \rightarrow \infty} x^{-6}$ (4 points)

10) Find $\lim_{x \rightarrow -\infty} 2^x$ (4 points)

11) Find $\lim_{x \rightarrow \infty} \frac{x^2+5}{x^2-3}$ (4 points)

12) Find $\lim_{x \rightarrow -\infty} \frac{-x^3+2x+4}{x^2-2x^3}$ (4 points)

13) Find the derivative of each of the functions below.

(a) $f(x) = 3x^5 - 2x^3$ (4 points)

(b) $f(x) = 7$ (4 points)

(c) $f(x) = \frac{x^2}{\sin(x)}$ (4 points)

14) Find the derivative of each of the functions below.

(d) $f(x) = 2^x \cdot 3^x$ (4 points)

(e) $\ln(x^{34})$ (4 points)

15) Given $f(x) = x^5$, which of the following expressions correctly give $f'(x)$? Circle all that apply. (3.5 points)

(a) $f'(x) = 5x^4$

(b) $f'(x) = 5x^4 \frac{dy}{dx}$

(c) $f'(x) = \lim_{h \rightarrow 0} \frac{(x+h)^5 - x^5}{h}$

(d) $f'(x) = \lim_{x \rightarrow 0} \frac{(x+h)^5 - x^5}{h}$

(e) $f'(x) = \lim_{h \rightarrow 0} \frac{(x+h)^5 - h^5}{h}$

(f) $f'(x) = \lim_{x \rightarrow 0} \frac{(x+h)^5 - h^5}{h}$

(g) $f'(x) = \lim_{b \rightarrow x} \frac{(x)^5 - b^5}{x - b}$

16) Find $\frac{dy}{dx}$, given that $xy^2 + \sin(y) = x^4 + 2$ (6 points)

17) The distance of a train from a station is given by $s(t) = \frac{1}{2}t^2$. How fast is the train traveling after 60 seconds? The function s is given in feet, while t is given in seconds. (6 points)

18) Use the graph of $y = f(x)$ below to find each of the following. (1 point each)

(a) $\lim_{x \rightarrow -4^-} f(x)$

(b) $\lim_{x \rightarrow -4^+} f(x)$

(c) $\lim_{x \rightarrow -4} f(x)$

(d) $\lim_{x \rightarrow -2^-} f(x)$

(e) $\lim_{x \rightarrow -2^+} f(x)$

(f) $\lim_{x \rightarrow -2} f(x)$

(g) $\lim_{x \rightarrow 1^-} f(x)$

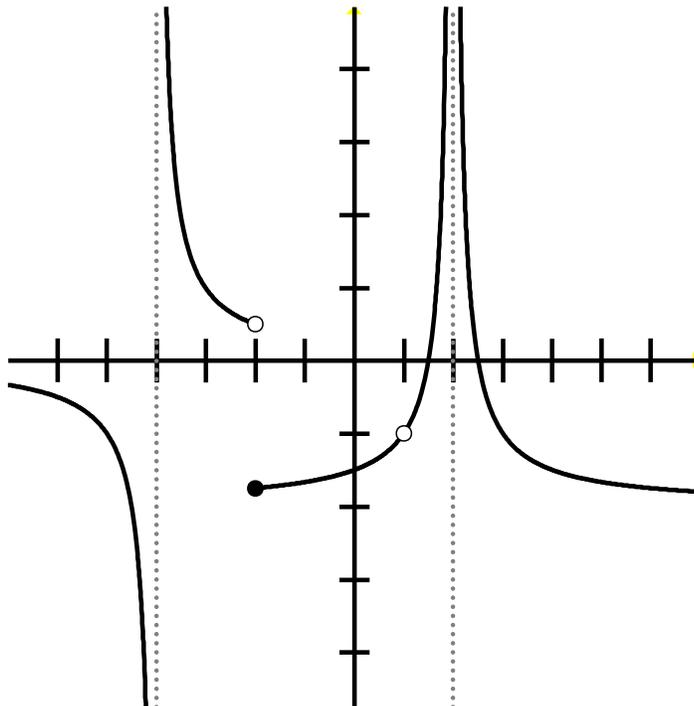
(h) $\lim_{x \rightarrow 1^+} f(x)$

(i) $\lim_{x \rightarrow 1} f(x)$

(j) $\lim_{x \rightarrow 2^-} f(x)$

(k) $\lim_{x \rightarrow 2^+} f(x)$

(l) $\lim_{x \rightarrow 2} f(x)$



19) This problem is intended to test your conceptual understanding of the formal definition of a limit. We covered this in class using what we called the “ $\varepsilon - \delta$ ” game. Below is a graph of a function. At $x = 2$, we think that the limit is $\lim_{x \rightarrow 2} f(x) = 3$. Today, our notion of closeness on the y -axis will be $\varepsilon = \frac{1}{2}$, so we must force $f(x)$ to be within $\frac{1}{2}$ units of 3. This is illustrated using the dotted lines on the graph below.

Find the corresponding notion of closeness on the x -axis that is required, and illustrate it on the graph. (6.5 points)

