

1 In each of the following, find $\frac{dy}{dx}$.

(A) $y = 3(x^5 + 3x^2 + 4x + 1)^9$

$$y' = 21(x^5 + 3x^2 + 4x + 1)^8 \cdot (5x^4 + 6x + 4)$$

(B) $x^2 + 3y^2 = 3x^3$

$$\begin{aligned} \frac{d}{dx}(x^2 + 3y^2) &= \frac{d}{dx}(3x^3) \\ 2x + 6yy' &= 9x^2 \\ 6yy' &= 9x^2 - 2x \\ y' &= \frac{9x^2 - 2x}{6y} \end{aligned}$$

2) A square concrete mold is increasing in size as the concrete fills the inside. If the side length is increasing at a rate of 2ft/min, how fast is the area of concrete changing when the square is 3 feet wide?

$$A = x^2$$

$$A' = 2xx'$$

$$x = 3$$

$$x' = 2$$

$$A' = 2 \cdot 3 \cdot 2 = 12 \text{ ft}^2/\text{min}$$

