

1) Let $\{a_n\}_{n=0}^{\infty}$ be the sequence defined by $a_n = 2n + 1$. Define a new sequence $\{b_k\}_{k=0}^{\infty}$ by taking every other term in the first sequence. That is, the new sequence is given by:

$$a_0, a_2, a_4, a_6, \dots$$

Find an explicit formula for b_k .

Relating a_n and b_k we see that:

$$b_0 = a_0$$

$$b_1 = a_2$$

$$b_2 = a_4$$

$$b_3 = a_6$$

Using that to relate n and k we see that $2k = n$. Plugging this into the formula we see that:

$$b_k = a_n = a_{2k} = 2(2k) + 1 = 4k + 1$$

2) Concatenate the string "abcd" with the string "gogg".

"abcdgogg"

3) Does your answer to #2 include the string "dog" as a substring?

No. There's only one d, so the substring starting with d would have to be the substring "dog". It is "dgo" which is not "dog".