Name Solutions Discrete I, Quiz 25

Use the code below to answer the following questions.

```
for i from 0 to n-1
"Line 2"
for j from 0 to n*n
    "Line 4"
    for k from 0 to i
    "Line 6"
```

1) If "Line 2" is the line of interest and everything else is trivial, what is the asymptotic growth rate of this algorithm?

O(n)

2) If "Line 4" is the line of interest and everything else is trivial, what is the asymptotic growth rate of this algorithm?

$$O(n \cdot n^2) = O(n^3)$$

Notice that the second loop has n^2 iterations!!

3) If "Line 6" is the line of interest and everything else is trivial, what is the asymptotic growth rate of this algorithm?

$$O(n^4)$$

At first glance maybe it's actually faster than this. If we the innermost loop actually ran n times we would get $\Theta(n^4)$ for sure. As is it requires a more in depth analysis, but indeed our intuition is accurate that actually is $\Theta(n^4)$

4) If "Line 2" and "Line 4" are the lines of interest and everything else is trivial, what is the asymptotic growth rate of this algorithm?

$$O(n+n^3) = O(n^3)$$

5) If "Line 4" and "Line 6" are the lines of interest and everything else is trivial, what is the asymptotic growth rate of this algorithm?

$$O(n^3 + n^4) = O(n^4)$$