

Name \_\_\_\_\_ Quiz 3

1) Given  $A = \{1,2,3\}$ ,  $B = \{2,3,4\}$ ,  $C = \{1,4,5,6\}$ , and  $D = \{3,6\}$  find the sets below. The universe is all positive integers less than 10.

$$A \cap B = \{2,3\}$$

$$B \cup D = \{2,3,4,6\}$$

$$A - C = \{2,3\}$$

$$A^c = \{4,5,6,7,8,9\}$$

$$B \times D = \{(2,3), (2,6), (3,3), (3,6), (4,3), (4,6)\}$$

2) Let  $A$  and  $B$  be sets. Prove that  $A \cap B \subseteq A$ .

Suppose  $x \in A \cap B$ . This means that  $x \in A$  and  $x \in B$ , In particular  $x \in A$ . Therefore by the definition of subset,  $A \cap B \subseteq A$

3) Let  $A$  and  $B$  be sets. Prove that  $(A \cup B = B) \Rightarrow A \subseteq B$

Suppose  $A \cup B = B$ . Now assume  $x \in A$ . Thus  $x \in A \cup B$ , and so the assumption that  $A \cup B = B$  tells us that also  $x \in B$ . Therefore  $A \subseteq B$