Consider the matrix given below.

$$[T] = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

1) Find a basis for the row space of [T].

2) Find a basis for the range of T.

3) Find a basis for the null space of [T]

4) What is the associated linear operator T?

5) Let $[T]^t$ denote the transpose of the matrix [T]. Find $[T]^t \cdot [T]$.