

1) Convert the decimal number 513 to base 5.

$$513 \div 5 = 102 \text{ R}3 \quad (\text{This remainder gives the one's place – what's left over after modding out by 5})$$

$$102 \div 5 = 20 \text{ R}2 \quad (\text{This remainder gives the five's place – what's left over after modding out by 25})$$

$$20 \div 5 = 4 \text{ R}0 \quad (\text{25's place})$$

$$4 \div 5 = 0 \text{ R}4 \quad (\text{125's place})$$

$$513 = (4023)_5$$

2) Show that $\sqrt{n^2 + 1}$ is $O(n)$.

$$\sqrt{n^2 + 1} \leq \sqrt{n^2 + n^2} = \sqrt{2n^2} \leq \sqrt{4n^2} = 2n$$

****Note that showing something is true requires mathematical reasoning. This is not the time to hand wave your ideas.**

3) Multiply $(1234)_5 \cdot (3002)_5$.

$$\begin{array}{r} 1234 \\ \times 3002 \\ \hline 3023 \\ 4312000 \\ 4320023 \end{array}$$